

# ACTION RULES & META ACTIONS



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## Introduction: Action Rule

An action rule /Ras & Wieczorkowska, PKDD 2000/ is a rule extracted from an information system that describes a possible transition of objects from one state to another with respect to a distinguished attribute called a decision attribute

#### **Information System**

| Α  | В  | D   |
|----|----|-----|
| a1 | b2 | ſτb |
| a2 | b2 |     |
| a2 | b2 | d2  |

#### **Assumption:**

- attributes are partitioned into stable and flexible

Values of attributes can be changed

## Introduction: Action Rule



conjunction of fixed condition features shared by both groups

proposed changes in values of flexible features

#### **Information System**

| Α  | В  | D  |
|----|----|----|
| a1 | b2 | d1 |
| a2 | b2 |    |
| a2 | b2 | d2 |

desired effect of the action

## Example

| X                     | a | b | C | d |
|-----------------------|---|---|---|---|
| $\mathbf{x}_1$        | 0 | S | 0 | L |
| $\mathbf{x}_2$        | 0 | R | 1 | L |
| $x_3$                 | 0 | S | 1 | L |
| x <sub>4</sub>        | 0 | R | 1 | L |
| <b>X</b> <sub>5</sub> | 2 | P | 2 | L |
| x <sub>6</sub>        | 2 | P | 2 | L |
| <b>x</b> <sub>7</sub> | 2 | S | 2 | Н |

{a, c} - stable attributes,{b, d} - flexible attributes,d - decision attribute.

Rules discovered:

$$r_1 = [ (b, P) \rightarrow (d, L)]$$

$$r_2 = [(a, 2) \land (b, S) \rightarrow (d, H)]$$

**Decision Table** 

Action rule:

$$[(\mathbf{a}, 2) \land (\mathbf{b}, P \rightarrow S)](\mathbf{x}) \Rightarrow [(\mathbf{d}, L \rightarrow H)](\mathbf{x})$$

## Application domain: Customer Attrition

#### **Facts:**

- On average, most US corporations lose half of their customers every five years (Rombel, 2001).
- **◆** Longer a customer stays with the organization, the more profitable he or she becomes (Pauline, 2000; Hanseman, 2004).
- The cost of attracting new customers is five to ten times more than retaining existing ones.
- About 14% to 17% of the accounts are closed for reasons that can be controlled like price or service (Lunt, 1993).

#### Action:

Reducing the outflow of the customers by 5% can double a typical company's profit (Rombel, 2001).





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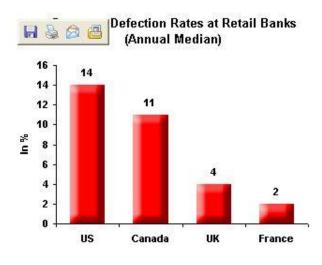
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### Customer Attrition in Retail Banking: US, Canada, UK, France

#### Report Published by Celent

Fighting customer attrition is a top priority at US and Canadian banks, and for good reason: customer defection rates are up to 7 times higher in the US and Canada than in Western Europe. A new Celent report explains why.



In a new report. "Customer Attrition in Retail Banking: the US. Canada, the UK, and France." Celent analyzes why customer defection rates are so much higher in the US and Canada than the UK and France.

The report, which is based on a survey of more than 30 banks, reviews trends affecting customer attrition in the UK and France, analyzes how Canadian and

American bankers have addressed attrition so far, and reports on their success. The report also suggests tactics that North American banks should pursue to get a 10% defection rate or better.

Over the past two years, half of top US and Canadian banks have seen their defection rates decrease by an average of 10%, while defection rates have remained the same for 40%. Only 10% have experienced increased attrition. The best organizations in the US and Canada have achieved a 12% customer defection rate.

























#### Methods for Action Rules Extraction:

- 1] Rule-based
  Prior extraction of classification rules is needed
  Example DEAR /Tsay & Ras, tree-based strategy/
- 2] Object-based
  Action rules are extracted directly from DB
  Example ARED /similar to Apriori/
- Ref 1: "Action rules discovery: System DEAR2, method and experiments", L.-S. Tsay, Z.W. Ras, Journal of Experimental and Theoretical Artificial Intelligence, Taylor & Francis, Vol. 17, No. 1-2, 2005, 119-128
- Ref 2: "Association Action Rules", Z.W. Ras, A. Dardzinska, L.-S. Tsay, H. Wasyluk, IEEE/ICDM Workshop on Mining Complex Data (MCD 2008), Pisa, Italy, ICDM Workshops Proceedings, IEEE Computer Society, 2008, 283-290

## **Action Rules Discovery (Preprocessing)**

#### Partition decision table S

Splitting the node using the stable attribute  $Dom(a) = \{1,2,3\}$  &  $Dom(b) = \{1,2,3,4,5\}$ 

| а | Ь | С | е | f | d |
|---|---|---|---|---|---|
| 2 | 1 | 1 | 7 | 8 | 1 |
| 2 | 5 | 4 | 6 | 8 | 1 |
| 1 | 1 | 4 | 9 | 4 | 2 |
| 1 | 4 | 5 | 8 | 7 | 2 |
| 2 | 1 | 5 | 2 | 8 | 3 |
| 2 | 1 | 4 | 2 | 8 | 3 |
| 1 | 2 | 4 | 7 | 1 | 2 |
| 2 | 1 | 1 | 6 | 8 | 1 |
| 3 | 2 | 4 | 6 | 8 | 2 |
| 3 | 3 | 5 | 7 | 4 | 2 |
| 3 | 3 | 5 | 6 | 2 | 3 |
| 2 | 5 | 4 | 6 | 8 | 3 |

#### Stable: { a, b}

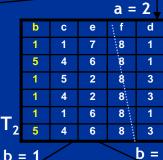
Flexible: {c, e, f}

**Reclassification direction:** 

 $2 \rightarrow 1 \text{ or } 3 \rightarrow 1$ 

|       |   |   |   |   | lacksquare |
|-------|---|---|---|---|------------|
|       | 9 | C | е | f | d          |
|       | 1 | 9 | 4 | 4 | 2          |
|       | 4 | 5 | 8 | 7 | 2          |
| $T_1$ | 2 | 4 | 7 | 1 | 2          |

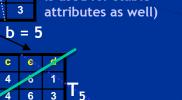
All objects have the same decision value, so this subtable is not analyzed any further



a = 1

All objects have the same value 8 for attribute f, so it is crossed out from the sub-table ( this condition is used for stable attributes as well)

a = 3



All the flexible values are the same for both objects, therefore this sub-table is not analyzed any further

|   | b | C | е | f | d |         |
|---|---|---|---|---|---|---------|
|   | 2 | 4 | 6 | 8 | 2 |         |
|   | 3 | 5 | 1 | 4 | 2 |         |
|   | 3 | 5 | 6 | 2 | 3 | $T_{3}$ |
| 4 |   |   |   |   |   |         |

None of the objects contain the desired class "1", so this subtable stops splitting any further

## DEAR - Rule-Based Action Rules Discovery

#### Set of rules R with supporting objects

| Objects        | a | b | c | d |
|----------------|---|---|---|---|
| x1, x2, x3, x4 | 0 |   |   | L |
| x1, x3         |   |   | 0 | L |
| x2, x4         |   | 2 |   | L |
| x2, x4         |   |   | 1 | L |
| x5, x6         |   | 3 |   | L |
| x7, x8         | 2 | 1 |   | H |
| x7, x8         |   | 1 | 2 | H |

Stable Attribute: {a, c}

Flexible Attribute: b

**Decision Attribute:** d

#### (d, L)-tree T2

| Objects        | a | b | c |
|----------------|---|---|---|
| x1, x2, x3, x4 | 0 |   |   |
| x1, x3         |   |   | 0 |
| x2, x4         |   | 2 |   |
| x2, x4         |   |   | 1 |
| x5, x6         |   | 3 |   |

#### (d, H)-tree T1

| Objects | a | b | c |
|---------|---|---|---|
| x7, x8  | 2 | 1 |   |
| x7, x8  |   | 1 | 2 |

| Objects | b | c |
|---------|---|---|
| x7, x8  | 1 |   |
|         |   |   |

| Objects | b | c |
|---------|---|---|
| x7, x8  | 1 | 2 |

| Objects | b |    |
|---------|---|----|
| x7, x8  | 1 | T2 |

c = 2

| Objects | b | c |
|---------|---|---|
| x1, x3  |   | 0 |
| x2, x4  | 2 |   |
| x2, x4  |   | 1 |
| x5, x6  | 3 |   |
|         |   |   |

c = 0

| x1, x2, x3, x4 |  |
|----------------|--|
| c = ?          |  |
|                |  |

**Objects** 

a = 0

b

**T6** 

| Objects        | b |
|----------------|---|
| x1, x2, x3, x4 |   |

| Objects | b |
|---------|---|
| x2, x4  | 2 |
| x5, x6  | 3 |

c = ?

| Objects | b |    |
|---------|---|----|
| x1, x3  |   | Τź |
| T3      |   |    |

| <b>Objects</b> | b |    |
|----------------|---|----|
| x2, x4         |   | TE |
|                |   | 15 |

(T3, T1) : (a = 2) 
$$\land$$
 (b, 2 $\rightarrow$ 1)  $\Rightarrow$  (d, L  $\rightarrow$  H)

$$(a = 2) \land (b, 3\rightarrow 1) \Rightarrow (d, L \rightarrow H)$$

## **ARED** - Object Based Action Rule Discovery

#### Decision System S

| X                     | а                     | Ь                     | С                     | d                     |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| <b>x</b> <sub>1</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>2</sub> | <u>a</u> 2            | <b>b</b> <sub>1</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>3</sub> | <b>a</b> <sub>2</sub> | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>4</sub> | <b>a</b> <sub>2</sub> | <b>b</b> <sub>1</sub> | <b>c</b> <sub>1</sub> | $d_1$                 |
| <b>X</b> <sub>5</sub> | <b>a</b> <sub>2</sub> | $\boldsymbol{b}_3$    | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>6</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>1</sub> | <b>c</b> <sub>2</sub> | $d_2$                 |
| <b>x</b> <sub>7</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>2</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>8</sub> | <b>a</b> <sub>1</sub> | <i>b</i> <sub>2</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>3</sub> |

$$sup(r) = \frac{2}{2}$$
  
 $conf(r) = \frac{2}{2} = 1$ 

$$(a, a_1 \rightarrow a_1)$$
  $(a,a_1)$   $Y = \{x_2, x_4\}$   
 $(a, a_2 \rightarrow a_2)$   $(a,a_2)$   $Z = \{x_1, x_2, x_3, x_4, x_5, x_7\}$   
 $(b, b_1 \rightarrow b_1)$   
 $(b, b_2 \rightarrow b_2)$  atomic action terms

$$(d, d_1 \rightarrow d_1)$$

$$(d, d_2 \rightarrow d_2)$$

$$r=[(a, a_2 \rightarrow a_2)^*(b, b_1 \rightarrow b_1)] \rightarrow (d, d_1 \rightarrow d_1)$$

$$(\mathsf{W},\,\mathsf{W})\in(\mathsf{Y},\,\mathsf{Y}\,)\to(\mathsf{W},\mathsf{W})\in(\mathsf{Z},\,\mathsf{Z})$$

action rule

Support:

$$\sup(r) = card(Y \cap Z)$$

Confidence:

$$conf(r) = \left[\frac{card(Y \cap Z)}{card(Y)}\right]$$

## Decision System S

| X                     | а                     | Ь                     | С                     | d                     |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| <b>x</b> <sub>1</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>x</b> <sub>2</sub> | $a_2$                 | <b>b</b> <sub>1</sub> | <i>c</i> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>3</sub> | $a_2$                 | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>4</sub> | $a_2$                 | <b>b</b> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>5</sub> | $a_2$                 | $\boldsymbol{b}_3$    | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>6</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>1</sub> | $c_2$                 | d <sub>2</sub>        |
| <b>x</b> <sub>7</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>2</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>8</sub> | <b>a</b> <sub>1</sub> | <i>b</i> <sub>2</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>3</sub> |

$$Y_1 = \{x_2, x_4\}$$
 $Z_1 = \{x_1, x_2, x_3, x_4, x_5, x_7\}$ 
 $Y_2 = \{x_1, x_6\}$ 
 $Z_2 = \{x_6\}$ 

$$\sup(r) = card(Y_1 \cap Z_1)$$

$$conf(r) = \left[\frac{card(Y_1 \cap Z_1)}{card(Y_1)}\right] * \left[\frac{card(Y_2 \cap Z_2)}{card(Y_2)}\right]$$

## Decision System S

| X                     | а                     | Ь                     | С                     | d                     |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| <b>x</b> <sub>1</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>2</sub> | $a_2$                 | <b>b</b> <sub>1</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>3</sub> | $a_2$                 | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>4</sub> | $a_2$                 | <b>b</b> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>5</sub> | <b>a</b> <sub>2</sub> | $\boldsymbol{b}_3$    | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>6</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>1</sub> | <b>c</b> <sub>2</sub> | d <sub>2</sub>        |
| <b>x</b> <sub>7</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>2</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>8</sub> | <b>a</b> <sub>1</sub> | <i>b</i> <sub>2</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>3</sub> |

$$Y_1 = \{x_2, x_4\}$$
 $Z_1 = \{x_1, x_2, x_3, x_4, x_5, x_7\}$ 
 $Y_2 = \{x_1, x_6\}$ 
 $Z_2 = \{x_6\}$ 

$$\sup(r) = \min\{ card(Y_1 \cap Z_1), card(Y_2 \cap Z_2) \}$$

$$conf(r) = \left[\frac{card(Y_1 \cap Z_1)}{card(Y_1)}\right] * \left[\frac{card(Y_2 \cap Z_2)}{card(Y_2)}\right]$$

#### $\lambda 1$ - minimum support, $\lambda 2$ - minimum confidence

Object reclassification from class  $d_1$  to  $d_2$   $\lambda 1=2$ ,  $\lambda 2=1/4$ 

$$\lambda 1 = 2, \lambda 2 = 1/4$$

| X                     | а                     | b                     | С                     | d                     |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| <b>X</b> <sub>1</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| X <sub>2</sub>        | $a_2$                 | <i>b</i> <sub>1</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>3</sub> | $a_2$                 | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>4</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>5</sub> | <b>a</b> <sub>2</sub> | $b_3$                 | $c_2$                 | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>6</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | <b>c</b> <sub>2</sub> | d <sub>2</sub>        |
| <b>x</b> <sub>7</sub> | a <sub>1</sub>        | <i>b</i> <sub>2</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>8</sub> | $a_1$                 | $b_2$                 | <b>c</b> <sub>1</sub> | $d_3$                 |

Meaning of  $(d,d_1 \rightarrow d_2)$  in S:

$$N_S(d,d_1 \rightarrow d_2) = [\{x_1,x_2, x_3, x_4, x_5, x_7\}, \{x_6\}]$$

**Atomic classification terms:** 

$$(b,b_1 \rightarrow b_1), (b,b_2 \rightarrow b_2), (b,b_3 \rightarrow b_3)$$
  
 $(a,a_1 \rightarrow a_2), (a,a_1 \rightarrow a_1), (a,a_2 \rightarrow a_2), (a,a_2 \rightarrow a_1)$   
 $(c,c_1 \rightarrow c_2), (c,c_2 \rightarrow c_1), (c,c_1 \rightarrow c_1), (c,c_2 \rightarrow c_2)$ 

stable attribute

flexible attributes

#### $\lambda 1$ - minimum support, $\lambda 2$ - minimum confidence

Object reclassification from class d<sub>1</sub> to d<sub>2</sub>

$$\lambda 1 = 2, \lambda 2 = 1/4$$

| X                     | а                     | b                     | С                     | d                     |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| <b>x</b> <sub>1</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | <b>C</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| X <sub>2</sub>        | $a_2$                 | <i>b</i> <sub>1</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>3</sub> | $a_2$                 | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>4</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>5</sub> | <b>a</b> <sub>2</sub> | $b_3$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>6</sub> | <i>a</i> <sub>1</sub> | <i>b</i> <sub>1</sub> | <i>c</i> <sub>2</sub> | d <sub>2</sub>        |
| <b>x</b> <sub>7</sub> | a <sub>1</sub>        | <i>b</i> <sub>2</sub> | $c_2$                 | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>8</sub> | $a_1$                 | $b_2$                 | <b>c</b> <sub>1</sub> | $d_3$                 |

#### **Notation:**

$$t_1=(b,b_1\to b_1), t_2=(b,b_2\to b_2), t_3=(b,b_3\to b_3),$$

$$t_4 = (a, a_1 \rightarrow a_2), t_5 = (a, a_1 \rightarrow a_1), t_6 = (a, a_2 \rightarrow a_2), t_7 = (a, a_2 \rightarrow a_1),$$

$$t_8 = (c, c_1 \rightarrow c_2), t_9 = (c, c_2 \rightarrow c_1), t_{10} = (c, c_1 \rightarrow c_1), t_{11} = (c, c_2 \rightarrow c_2),$$

$$t_{12} = (d, d_1 \rightarrow d_2).$$

stable attribute

flexible attributes

| Х                     | а                     | b                     | С                     | d                     |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| <b>X</b> <sub>1</sub> | <i>a</i> <sub>1</sub> | <i>b</i> <sub>1</sub> | <b>C</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>2</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | $c_2$                 | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>3</sub> | <b>a</b> <sub>2</sub> | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>4</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>5</sub> | <b>a</b> <sub>2</sub> | $b_3$                 | $c_2$                 | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>6</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | $c_2$                 | $d_2$                 |
| <b>X</b> <sub>7</sub> | <i>a</i> <sub>1</sub> | <i>b</i> <sub>2</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>8</sub> | <i>a</i> <sub>1</sub> | <i>b</i> <sub>2</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>3</sub> |

$$\sup(r) = card(Y_1 \cap Z_1)$$

For decision attribute in S:

$$N_{S}(d,d_{1} \rightarrow d_{2}) = [\{x_{1},x_{2}, x_{3}, x_{4}, x_{5}, x_{7}\}, \{x_{6}\}]$$

For classification attribute in S:

Not marked λ1=3

Mark "-" λ2=0

Mark "-" λ1=1

Mark "-" λ2=0

$$N_{S}(t_{1}) = N_{S}(b,b_{1}\rightarrow b_{1}) = [\{x_{1},x_{2}, x_{4}, x_{6}\}, \{x_{1},x_{2}, x_{4}, x_{6}\}]$$
  
 $N_{S}(t_{2}) = N_{S}(b,b_{2}\rightarrow b_{2}) = [\{x_{3},x_{7}, x_{8}\}, \{x_{3},x_{7}, x_{8}\}]$   
 $N_{S}(t_{3}) = N_{S}(b,b_{3}\rightarrow b_{3}) = [\{x_{5}\}, \{x_{5}\}]$   
 $N_{S}(t_{4}) = N_{S}(a,a_{1}\rightarrow a_{2}) = [\{x_{1},x_{6}, x_{7}, x_{8}\}, \{x_{2},x_{3}, x_{4}, x_{5}\}]$ 

| X                     | а                     | ь                     | С                     | d                     |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| <b>X</b> <sub>1</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>2</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | <i>c</i> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>3</sub> | <b>a</b> <sub>2</sub> | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>4</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>5</sub> | $a_2$                 | $b_3$                 | $c_2$                 | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>6</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | <b>c</b> <sub>2</sub> | $d_2$                 |
| <b>x</b> <sub>7</sub> | <i>a</i> <sub>1</sub> | <i>b</i> <sub>2</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>8</sub> | $a_1$                 | <i>b</i> <sub>2</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>3</sub> |

For decision attribute in S:

$$N_S(d,d_1 \rightarrow d_2) = [\{x_1,x_2, x_3, x_4, x_5, x_7\}, \{x_6\}]$$

For classification attribute in S:

Not marked  $\lambda 1=2$ 

Mark "-"  $\lambda 2 = 0$ 

Mark "+"  $\lambda 1 = 4, \lambda 2 = 1/4$ 

$$N_{S}(t_{5}) = N_{S}(a, a_{1} \rightarrow a_{1}) = [\{x_{1}, x_{6}, x_{7}, x_{8}\}, \{x_{1}, x_{6}, x_{7}, x_{8}\}]$$

$$N_{S}(t_{6}) = N_{S}(a, a_{2} \rightarrow a_{2}) = [\{x_{2}, x_{3}, x_{4}, x_{5}\}, \{x_{2}, x_{3}, x_{4}, x_{5}\}]$$

$$N_{S}(t_{7})=N_{S}(a,a_{2}\rightarrow a_{1})=[\{x_{2},x_{3},x_{4},x_{5}\},\{x_{1},x_{6},x_{7},x_{8}\}]$$

| X                     | а                     | Ь                     | С                     | d                     |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| <b>X</b> <sub>1</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | d <sub>1</sub>        |
| <b>X</b> <sub>2</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | <i>c</i> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>3</sub> | $a_2$                 | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>4</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>5</sub> | <b>a</b> <sub>2</sub> | $b_3$                 | $c_2$                 | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>6</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | $c_2$                 | $d_2$                 |
| <b>x</b> <sub>7</sub> | a <sub>1</sub>        | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>8</sub> | <i>a</i> <sub>1</sub> | <i>b</i> <sub>2</sub> | <b>c</b> <sub>1</sub> | <b>d</b> <sub>3</sub> |

Object reclassification from class d1 to d2

$$\lambda 1=2, \lambda 2=1/4$$

For decision attribute in S:

$$N_{S}(t_{12})=[\{x_{1},x_{2}, x_{3}, x_{4}, x_{5}, x_{7}\}, \{x_{6}\}]$$

For classification attribute in S:

Not marked 
$$\lambda 1=3$$
  $N_{5}(t_{1})=[\{x_{1},x_{2},x_{4},x_{6}\},\{x_{1},x_{2},x_{4},x_{6}\}]$   
Marked "-"  $\lambda 2=0$   $N_{5}(t_{2})=[\{x_{3},x_{7},x_{8}\},\{x_{3},x_{7},x_{8}\}]$   
Marked "-"  $\lambda 1=1$   $N_{5}(t_{3})=[\{x_{5}\},\{x_{5}\}]$   
Marked "-"  $\lambda 2=0$   $N_{5}(t_{4})=[\{x_{1},x_{6},x_{7},x_{8}\},\{x_{2},x_{3},x_{4},x_{5}\}]$   
Not marked  $\lambda 1=2$   $N_{5}(t_{5})=[\{x_{1},x_{6},x_{7},x_{8}\},\{x_{1},x_{6},x_{7},x_{8}\}]$   
Marked "-"  $\lambda 2=0$   $N_{5}(t_{6})=[\{x_{2},x_{3},x_{4},x_{5}\},\{x_{2},x_{3},x_{4},x_{5}\}]$   
Mark "+"  $\lambda 1=4$ ,  $\lambda 2=1/4$   $N_{5}(t_{7})=[\{x_{2},x_{3},x_{4},x_{5}\},\{x_{1},x_{6},x_{7},x_{8}\}]$ 

| X                     | а                     | Ь                     | c                     | d                     |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| <b>x</b> <sub>1</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | $d_1$                 |
| <b>X</b> <sub>2</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | <i>c</i> <sub>2</sub> | $d_1$                 |
| <b>X</b> <sub>3</sub> | $a_2$                 | $b_2$                 | <i>c</i> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>4</sub> | $a_2$                 | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | $d_1$                 |
| <b>X</b> <sub>5</sub> | <b>a</b> <sub>2</sub> | $b_3$                 | <i>c</i> <sub>2</sub> | $d_1$                 |
| <b>X</b> <sub>6</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | <b>c</b> <sub>2</sub> | $d_2$                 |
| <b>x</b> <sub>7</sub> | a <sub>1</sub>        | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |
| <b>X</b> <sub>8</sub> | <i>a</i> <sub>1</sub> | <i>b</i> <sub>2</sub> | <b>c</b> <sub>1</sub> | $d_3$                 |

Object reclassification from class d1 to d2  $\lambda_{1=2}$ ,  $\lambda_{2=1/4}$ 

For decision attribute in S:

$$N_{S}(t_{12})=[\{x_{1},x_{2}, x_{3}, x_{4}, x_{5}, x_{7}\}, \{x_{6}\}]$$

For classification attribute in S:

 $conf = 2/3 *1/5 < \lambda_2$ 

| Not marked | $N_{S}(t_{8})=N_{S}(c,c_{1}\rightarrow c_{2})=[\{x_{1},x_{4},x_{8}\},\{x_{2},x_{3},x_{5},x_{6},x_{7}\}]$            |
|------------|---|
| Marked "-" | $N_{S}(t_{9}) = N_{S}(c,c_{2}\rightarrow c_{1}) = [\{x_{2}, x_{3}, x_{5}, x_{6}, x_{7}\}, \{x_{1}, x_{4}, x_{8}\}]$ |
| Marked "-" | $N_{S}(t_{10}) = N_{S}(c,c_{1} \rightarrow c_{1}) = [\{x_{1}, x_{4}, x_{8}\}, \{x_{1}, x_{4}, x_{8}\}]$             |
| Not marked | $N_{S}(t_{11}) = N_{S}(c, c_{2} \rightarrow c_{2}) =$   |
|            | $[\{X_2, X_3, X_5, X_6, X_7\}, \{X_2, X_3, X_5, X_6, X_7\}]$  |

#### Object reclassification from class d1 to d2

 $\lambda 1 = 2, \ \lambda 2 = 1/4$ 

Now action terms of length 2 from unmarked action terms of length 1

#### For decision attribute in S:

$$N_{S}(t_{12})=[\{x_{1},x_{2}, x_{3}, x_{4}, x_{5}, x_{7}\}, \{x_{6}\}]$$

#### For classification attribute in S:

$$N_{S}(t_{1})=[\{x_{1},x_{2}, x_{4}, x_{6}\}, \{x_{1},x_{2}, x_{4}, x_{6}\}], N_{S}(t_{5})=[\{x_{1},x_{6}, x_{7}, x_{8}\}, \{x_{1},x_{6}, x_{7}, x_{8}\}],$$

$$N_{S}(t_{8})=[\{x_{1},x_{4}, x_{8}\}, \{x_{2}, x_{3}, x_{5}, x_{6}, x_{7}\}], N_{S}(t_{11})=[\{x_{2}, x_{3}, x_{5}, x_{6}, x_{7}\}, \{x_{2}, x_{3}, x_{5}, x_{6}, x_{7}\}].$$

$$N_{S}(t_{1}^{*}t_{5})=[\{x_{1}, x_{6}\}, \{x_{1}, x_{6}\}]$$

$$N_{S}(t_{1}^{*}t_{8})=[\{x_{1}, x_{4}\}, \{x_{2}, x_{6}\}]$$

#### Rule $r = [t_1 * t_8 \rightarrow t_{12}]$ , conf = $1/2 \ge \lambda_2$ , sup= $2 \ge \lambda_2$

$$N_{S}(t_{1}^{*}t_{11})=[\{x_{2}, x_{6}\}, \{x_{2}, x_{6}\}]$$

$$N_5(t_5*t_8)=[\{x_1, x_8\}, \{x_6, x_7\}]$$

$$N_{S}(t_{5}^{*}t_{11})=[\{x_{6}, x_{7}\}, \{x_{6}, x_{7}\}]$$

$$N_{S}(t_{8}^{*}t_{11})=[\emptyset, \{x_{2}, x_{3}, x_{5}, x_{6}, x_{7}\}]$$

## **ARED**

Object reclassification from class d1 to d2

$$\lambda 1 = 2, \lambda 2 = 1/4$$

#### For decision attribute in S:

$$N_{S}(t_{12})=[\{x_{1},x_{2}, x_{3}, x_{4}, x_{5}, x_{7}\}, \{x_{6}\}]$$

#### For classification attribute in S:

#### **Action rules:**

$$[[(b,b1\rightarrow b1)^*(c,c1\rightarrow c2)] \rightarrow (d, d1\rightarrow d2)]$$
$$[[(a,a2\rightarrow a1] \rightarrow (d, d1\rightarrow d2)]$$

| X                     | а                     | Ь                     | С                     | d                     |  |  |
|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|--|--|
| <b>x</b> <sub>1</sub> | a <sub>1</sub>        | <i>b</i> <sub>1</sub> | <b>c</b> <sub>1</sub> | $d_1$                 |  |  |
| <b>x</b> <sub>2</sub> | $a_2$                 | <b>b</b> <sub>1</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |  |  |
| <b>X</b> <sub>3</sub> | <b>a</b> <sub>2</sub> | <b>b</b> <sub>2</sub> | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |  |  |
| <b>X</b> <sub>4</sub> | <b>a</b> <sub>2</sub> | <i>b</i> <sub>1</sub> | <b>C</b> <sub>1</sub> | $d_1$                 |  |  |
| <b>X</b> <sub>5</sub> | $a_2$                 | $b_3$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |  |  |
| <b>X</b> <sub>6</sub> | <b>a</b> <sub>1</sub> | <b>b</b> <sub>1</sub> | <b>c</b> <sub>2</sub> | $d_2$                 |  |  |
| <b>x</b> <sub>7</sub> | <b>a</b> <sub>1</sub> | $b_2$                 | <b>c</b> <sub>2</sub> | <b>d</b> <sub>1</sub> |  |  |
| <b>X</b> <sub>8</sub> | <b>a</b> <sub>1</sub> | <i>b</i> <sub>2</sub> | <b>c</b> <sub>1</sub> | $d_3$                 |  |  |

#### **Atomic Action Terms:**

1.  $(a, a_1 \rightarrow a_2)$ , where a is symbolic attribute

attribute

$$a_1$$
,  $a_2 \in V_a$ 

if  $a_1 = a_2$  then a - stable on  $a_1$ 

- 2.  $(a, [a_1, a_2] \uparrow [a_3, a_4])$ , where a is numerical,  $a_1 \le a_2 < a_3 \le a_4$ , and  $a_i \in V_a$
- 3.  $(a, [a_1, a_2] \downarrow [a_3, a_4])$ , where a is numerical,  $a_1 \le a_2 < a_3 \le a_4$ , and  $a_i \in V_a$
- ↑ value is increased; ↓ value is decreased

Candidate action set - any collection of atomic actions

Action set - candidate action set which does not contain two atomic actions referring to the same attribute

Example:  $\{(b, b_2), (b, [b_1, b_2] \uparrow [b_3, b_4])\}$  – candidate action set but not action set.

Action term - conjunction of atomic actions forming an action set.

Example:  $(a, a_2) \land (c, c_1 \rightarrow c_2) \land (b, [b_1, b_2] \uparrow [b_3, b_4])$ 

#### Interpretation $N_S$ of action terms in S=(X,A,V):

$$N_{S}((a, a_{1} \rightarrow a_{2})) = [\{x \in X : a(x) = a_{1}\}, \{x \in X : a(x) = a_{2}\}].$$

$$N_{S}((a, [a_{1}, a_{2}] \downarrow [a_{3}, a_{4}])) = [\{x \in X : a_{1} \leq a(x) \leq a_{2}\}, \{x \in X : a_{3} \leq a(x) \leq a_{4}\}]$$

$$N_{S}((a, [a_{1}, a_{2}] \uparrow [a_{3}, a_{4}])) = [\{x \in X : a_{1} \leq a(x) \leq a_{2}\}, \{x \in X : a_{3} \leq a(x) \leq a_{4}\}]$$

$$N_{S}((a, \uparrow [a_{3}, a_{4}])) = [\{x \in X : a(x) < a_{3}\}, \{x \in X : a_{3} \leq a(x) \leq a_{4}\}]$$

$$N_{S}((a, [a_{3}, a_{4}] \uparrow)) = [\{x \in X : a_{3} \leq a(x) \leq a_{4}\}, \{x \in X : a_{4} < a(x)\}]$$

Information System S=(X, A, V)

Action Rule: 
$$r = [t \rightarrow t']$$
  $t = t_1 \land t_2 \land ... \land t_k$ 

$$N_S(t) = [Y_1, Y_2]$$
  $N_S(t') = [Z_1, Z_2]$ 

Support:

$$\sup(r) = \min\{ \ card(Y_1 \cap Z_1), card(Y_2 \cap Z_2) \}$$

Atomic actions

Confidence: 
$$conf(r) = \left[\frac{card(Y_1 \cap Z_1)}{card(Y_1)}\right] \cdot \left[\frac{card(Y_2 \cap Z_2)}{card(Y_2)}\right]$$

#### Meta-actions /A. Tuzhilin (2006)/

Actions which trigger changes of flexible attributes either directly or indirectly because of correlations among certain attributes in the system.

**Example 1:** Taking a drug /Lamivudine is used for treatment of chronic hepatitis B. It *improves the seroconversion of e-antigen positive hepatitis B* and also *improves histology staging of the liver* but at the same time it can cause a number of other symptoms. This is why doctors have to order certain lab tests to check patient's response to that drug.

**Example 2:** Classification attributes are: *Explain difficult concepts effectively, Stimulate student interest in the course, Provide sufficient feedback.*Meta-actions: Change the content of the course, Change the textbook of the course, ...

## **Action Rules - continuation**

**Influence Matrix** 

$$A_1, A_2, A_3, ..., A_m$$
 – attributes  $M_1, M_2, M_3, ..., M_n$  – meta actions  $E_{ij}$  – atomic action or NULL,  $i \le m, j \le n$ 

|       | $\mathbf{A}_{1}$ | $\mathbf{A}_2$  | $A_3$    | $A_4$           | •••• | $\mathbf{A}_{\mathrm{m}}$  |
|-------|------------------|-----------------|----------|-----------------|------|----------------------------|
| $M_1$ | E <sub>11</sub>  | E <sub>12</sub> | $E_{13}$ | E <sub>14</sub> |      | E <sub>1m</sub>            |
| $M_2$ | $E_{21}$         | $E_{22}$        | $E_{23}$ | E <sub>24</sub> |      | $E_{2m}$                   |
| $M_3$ | $E_{31}$         | $E_{32}$        | $E_{33}$ | $E_{34}$        |      | $E_{3m}$                   |
| $M_4$ | $E_{41}$         | $E_{42}$        | $E_{43}$ | E <sub>44</sub> |      | $\mathrm{E}_{4\mathrm{m}}$ |
|       |                  |                 |          |                 |      |                            |
| $M_n$ | $E_{m1}$         | $E_{m2}$        | $E_{m3}$ | $E_{m4}$        |      | $E_{mn}$                   |

Atomic actions triggered by  $M_3$ 

Action rule:  $r = [t \Rightarrow (d, d_1 \rightarrow d_2)]$ , where t – action term

## **Action Rules - continuation**

Meta-actions based decision system  $S(d)=(X,A\cup\{d\},V)$ ,

|       | $\mathbf{A}_1$    | $\mathbf{A}_2$ | $\mathbf{A}_3$ | $\mathbf{A}_4$  | <br>A <sub>m</sub> |
|-------|-------------------|----------------|----------------|-----------------|--------------------|
| $M_1$ | E <sub>11</sub>   | $E_{12}$       | $E_{13}$       | Null            | $E_{1m}$           |
| $M_2$ | Null              | $E_{22}$       | $E_{23}$       | E <sub>24</sub> | $E_{2m}$           |
| $M_3$ | $E_{31}$          | $E_{32}$       | Null           | Null            | Null               |
| $M_4$ | $\mathrm{E}_{41}$ | Nul            | $E_{43}$       | E <sub>44</sub> | $E_{4m}$           |
|       |                   |                |                |                 |                    |
| $M_n$ | $E_{m1}$          | Null           | $E_{m3}$       | $E_{m4}$        | $E_{mn}$           |

with 
$$A = \{A_1, A_2, ..., A_m\}$$

Influence Matrix

Meta-action M<sub>3</sub> triggers two atomic actions:

$$\{E_{32} = [a_2 \rightarrow a_2'], E_{31} = [a_1 \rightarrow a_1']\}$$

Candidate action rule -

$$r = [(A_1, a_1 \rightarrow a_1') \land (A_2, a_2 \rightarrow a_2') \land (A_4, a_4 \rightarrow a_4')]) \Rightarrow (d, d_1 \rightarrow d_1')$$

We say that r is valid in S with respect to meta-action  $M_3$  if the atomic actions triggered by  $M_3$  do not contradict with atomic actions in r.

## **Action Rules - continuation**

Meta-actions based decision system  $S(d)=(X,A\cup\{d\},V)$ ,

| with | A= | $[A_1,A_2,\ldots,A_m]$ | } |
|------|----|------------------------|---|
|------|----|------------------------|---|

|                | <b>A</b> <sub>1</sub> | A <sub>2</sub>  | <b>A</b> <sub>3</sub> | A <sub>4</sub>  | •••• | $A_{\rm m}$                |
|----------------|-----------------------|-----------------|-----------------------|-----------------|------|----------------------------|
| $\mathbf{M}_1$ | $E_{11}$              | E <sub>12</sub> | $E_{13}$              | E <sub>14</sub> |      | $\rm E_{1m}$               |
| $\mathrm{M}_2$ | $E_{21}$              | $E_{22}$        | $E_{23}$              | E <sub>24</sub> |      | $E_{2m}$                   |
| $M_3$          | $E_{31}$              | $E_{32}$        | $E_{33}$              | E <sub>34</sub> |      | $E_{3m}$                   |
| $M_4$          | $E_{41}$              | $E_{42}$        | $E_{43}$              | E <sub>44</sub> |      | $\mathrm{E}_{4\mathrm{m}}$ |
| • • • • •      |                       |                 |                       |                 |      |                            |
| $M_n$          | $E_{m1}$              | $E_{m2}$        | $E_{m3}$              | $E_{m4}$        |      | $E_{mn}$                   |

**Influence Matrix** 

We say that action rule r extracted from S(d) is supported by meta-actions in  $M=\{M_{i1}, M_{i2}, ..., M_{in}\}$ , if r is valid in S with respect to each meta-action in M and each atomic action at the left-hand side of r is triggered by minimum one meta-action in M.

## **Action Rules Discovery - Example**

|                | a                     | b     | c                     |
|----------------|-----------------------|-------|-----------------------|
| $M_1$          |                       | $b_1$ | $c_2 \rightarrow c_1$ |
| $\mathrm{M}_2$ | $a_2 \rightarrow a_1$ | $b_2$ |                       |
| $M_3$          | $a_1 \rightarrow a_2$ |       | $c_2 \rightarrow c_1$ |
| $M_4$          |                       | $b_1$ | $c_1 \rightarrow c_2$ |
| $\mathrm{M}_5$ |                       |       | $c_1 \rightarrow c_2$ |
| $M_6$          | $a_1 \rightarrow a_2$ |       | $c_1 \rightarrow c_2$ |

Influence Matrix for S(d)

#### Candidate action rules:

 $r_1 = [[(b, b_1) \land (c, c_1 \rightarrow c_2)]) \Rightarrow (d, d_1 \rightarrow d_2)], \text{ valid with respect to } M_4, M_5, M_6$  $r_2 = [(a, a_2 \rightarrow a_1)) \Rightarrow (d, d_1 \rightarrow d_2)], \text{ valid with respect to } M_2, M_4, M_5 \text{ but not valid with respect to } M_2$ 

## **Application Domain**

## Database HEPAR (Medical Center of Postgraduate Education, Warsaw, Poland) prepared by Dr. med. Hanna Wasyluk

758 patients described by 106 attributes (including 31 laboratory tests with values discretized to: "below normal", "normal", "above normal"). 14 attributes are stable. Two tests are invasive tests: HBsAg [in tissue], HBcAg [in tissue]. There are 7 decision values (attribute d):

I. Acute hepatitis

IIa. Subacute hepatitis (types BC)

IIb. Subacute hepatitis (alcohol-abuse)

IIIa. Chronic hepatitis (curable)

IIIb. Chronic hepatitis (non-curable)

IV. Cirrhosis hepatitis

V. Liver cancer

We ask for re-classifications: IIb  $\rightarrow$  I, IIIa  $\rightarrow$  I

## **Application Domain**

#### Chosen d-reduct has no invasive tests, 11% incomplete data

 $\{m, n, q, u, y, aa, ah, ai, am, an, aw, bb, bg, by, cj, cm\}$ 

```
Bleeding
m
      Subjaundice symptoms
n
      Eructation
q
      Obstruction
u
      Weight loss
y
      Smoking
aa
      History of viral hepatitis (stable)
ah
      Surgeries in the past (stable)
ai
      History of hospitalization (stable)
am
      Jaundice in pregnancy
an
      Erythematous dermatitis
aw
bb
      Cysts
      Sharp liver edge (stable)
bg
      Blood cell plaque
bm
      Alkaline phosphatase
by
      Prothrombin index
cj
      Total cholesterol
cm
      Decision attribute
```

## Application Domain: Database HEPAR

- No history of viral hepatitis but with history of surgery and hospitalization, sharp
- liver edge normal, no subjaundice symptoms, total cholesterol normal,
  - erythematous dermatitis normal, weight normal, no cysts, patient does not smoke

$$[(ah=1) \land (ai=2) \land (am=2) \land (bg=1)] \land (cm=1) \land (aw=1) \land (u, \rightarrow 1) \land (bb=1) \land (aa=1) \land (q, \rightarrow 1) \land (m, \rightarrow 1) \land (n=1) \land (bm, \rightarrow up) \land (y=1) \land (by, \rightarrow up) \rightarrow (d, IIIa \rightarrow I)$$

$$\begin{array}{c} [(ah=1) \land (ai=2) \land (am=2) \land (bg=1)] \land (cm=1) \land (aw=1) \land (u, \rightarrow 1) \land (bb=1) \land (aa=1) \\ \land (q, \rightarrow 1) \land (m, \rightarrow 1) \land (n=1) \land (bm, \rightarrow up) \land (y=1) \land (by, \rightarrow down) \\ & \rightarrow (d, IIIa \rightarrow I) \end{array}$$

Two quite similar action rules have been constructed:

By getting rid of obstruction, eructation, bleeding, by decreasing the blood cell plaque and by changing the level of alkaline phosphatase we should be able reclassify the patient from IIIa group to I.

Attribute values of total cholesterol, weight, and smoking have to stay unchanged.

## Cost of Meta Action Rules

Meta Actions (drugs)

#### Action Rule II requires getting rid of:

```
    obstruction (u)
    eructation (q)
    bleeding (m)
    decreased blood cell plaque (bm)
    increased level of alkaline phosphatase (by)
    HEPATIL HEPARGEN
    HEPATIL HEPARGEN
    HEPATIL HEPARGEN
```

```
 [(ah=1) \land (ai=2) \land (am=2) \land (bg=1)] \land (cm=1) \land (aw=1) \land (u, \rightarrow 1) \land (bb=1) \land (aa=1) \land (q, \rightarrow 1) \land (m, \rightarrow 1) \land (n=1) \land (bm, \rightarrow up) \land (y=1) \land (by, \rightarrow down) \rightarrow (d, IIIa \rightarrow I)
```

\_\_\_\_\_

```
[(ah=1)\land (ai=2)\land (am=2)\land (bg=1)]\land (cm=1)\land (aw=1)\land (bb=1)\land (aa=1)\land (n=1)\land (y=1)\land [obstruction, eructation, bleeding, increased blood cell plaque, increased level of alkaline phosphatase ] <math>\land [Take HEPATIL] \rightarrow (d, IIIa \rightarrow I)
```

 $[(ah=1)\land (ai=2)\land (am=2)\land (bg=1)]\land (cm=1)\land (aw=1)\land (bb=1)\land (aa=1)\land (n=1)\land (y=1)\land [obstruction, eructation, bleeding, increased blood cell plaque, increased level of alkaline phosphatase ] <math>\land$  [Take HEPERGEN & TRIPHALA]  $\rightarrow$  (d, IIIa  $\rightarrow$  I)

```
(a, a_1 \rightarrow a_2) - atomic action set cost((a, a_1 \rightarrow a_2)) - cost of action expecting to change value of attribute a from a_1 to a_2. t_1 = (a, a_1 \rightarrow a_2), \ t_2 = (b, b_1 \rightarrow b_2) - two atomic action sets t_1, t_2 are positively correlated if changes t_1, t_2 support each other
```

Change  $t_1$  implies change  $t_2$  and  $t_2$  implies change  $t_1$ .

#### **Definition:**

Let  $t = t_1 * t_2 * ... * t_m$  is a frequent action set, where each  $t_i$  - atomic action set.

```
Let T = \{t_1, t_2, ..., t_m\} and:

t_i \sim t_j iff t_i and t_j are positively correlated.
```

Equivalence relation, partitions T into equivalence classes  $(T = T_1 \cup T_2 \cup ... \cup T_k)$ 

#### **Definition:**

Let  $t = t_1 * t_2 * ... * t_m$  is a frequent action set, where each  $t_i$  - atomic action set.

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 and:  
 $t_i \sim t_j$  iff  $t_i$  and  $t_j$  are positively correlated.

#### Now:

In each equivalence class  $T_i$ , an atomic action set  $a(T_i)$  of the lowest cost is identified.

The cost of t is defined as:  $cost(t) = \sum \{cost(a(T_i)): 1 \le i \le k\}$ 

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#### Now:

The cost of t is defined as:  $cost(t) = \sum \{cost(a(T_i)): 1 \le i \le k\}$ 

$$a(T_1)*a(T_2)*...*a(T_k) \rightarrow [t-\{a(T_i)\colon 1\le i\le k\}]$$
 - simple association action rule.

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 and:  
 $t_i \sim t_j$  iff  $t_i$  and  $t_j$  are positively correlated.

Now:

The cost of t is defined as:  $cost(t) = \sum \{cost(a(T_i)): 1 \le i \le k\}$ 

$$r = [a(T_1) * a(T_2) * ... * a(T_k) \rightarrow [t - \{a(T_i): 1 \le i \le k\}]]$$
 - simple association action rule.

The cost of r is defined as the cost of  $a(T_1) * a(T_2) * ... * a(T_k)$ 

## **Some Publications**

"Application of Action Rules to HEPAR Clinical Decision Support System", H. Wasyluk, Z.W. Ras, E. Wyrzykowska, in Experimental and Clinical Hepatology Journal, Vol. 4, No. 2, 2008

"Action Rules Discovery based on Tree Classifiers and Meta-Actions", Z. Ras, A. Dardzinska, in Foundations of Intelligent Systems, Proceedings of ISMIS'09, (Eds. J. Rauch et al), LNAI, Vol. 5722, Springer, 2009, 66-75

"Action Rule Discovery From Incomplete Data", S. Im, Z.W. Ras, H. Wasyluk, in Knowledge and Information Systems Journal, Springer, 2009

"Association Action Rules", Z.W. Ras, A. Dardzinska, L.-S. Tsay, H. Wasyluk, IEEE/ICDM Workshop on Mining Complex Data (MCD 2008), Pisa, Italy, ICDM Workshops Proceedings, IEEE Computer Society, 2008, 283-290

"Action Rules Discovery without pre-existing classification rules", Z.W. Ras, A. Dardzinska, in *Proceedings of RSCTC 2008 Conference*, Akron, Ohio, LNAI 5306, Springer, 2008, 181-190

# Questions?



Thank You